

## Key Stage 1 Addition and Subtraction Calculation Policy

Addition EYFS		Manipulatives	Subtraction EYFS		
Pictorial			Pictorial		
		Counters Numicon Multi-link Compare bears Fingers Any objects 			
Addition Year 1			Subtraction Year 1		
Pictorial	Abstract	Manipulatives		Pictorial	Abstract
2 people are on the bus. 5 more get on at the next stop. How many people are on the bus now? <b>[Might be recorded as: <math>2 + 5 = 7</math>]</b>		Counters Number lines Numicon Multi-link Compare bears Fingers 	Mum baked 13 biscuits. I ate 8. How many were left? <b>[Might be recorded as: <math>13 - 8 = 5</math>]</b>		
Cubes/counters/dots/multi-link: 			Cubes/counters/dots/multi-link: 		

## Addition Year 2

Pictorial

Abstract

## Manipulatives

## Subtraction Year 2

Pictorial

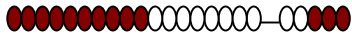
Abstract

Counters  
Number lines  
Numicon  
Multi-link  
Dienes  
Stringed beads

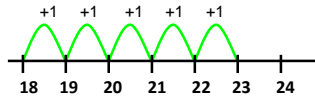


$$18 + 5 = 23$$

Beads:

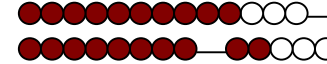


Number line:

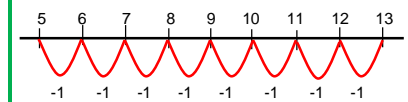


$$13 - 8 = 5$$

Beads:

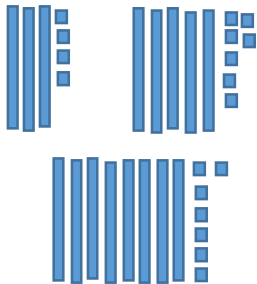


Number line:

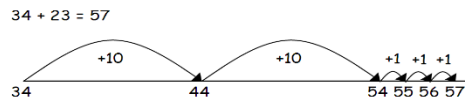


$$34 + 23 = 57$$

Dienes:



Number line:

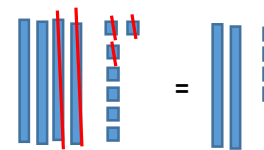


Partitioning:

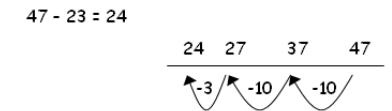
$$\begin{array}{r} 34 + 23 = 57 \\ \begin{array}{l} 30 + 20 = 50 \\ 4 + 3 = 7 \\ 50 + 7 = 57 \end{array} \end{array}$$

$$47 - 23 = 24$$

Dienes:

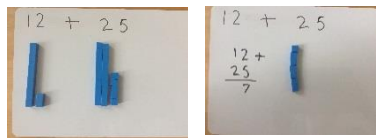


Number line:



## Introduced by the end of Year 2

$$12 + 25 = 37$$



**Column Addition**

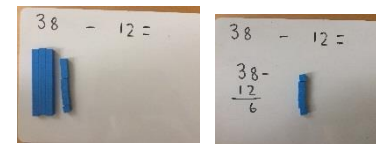
Model partitioning for expanded written method first.

$$\begin{array}{r} 12 \\ + 25 \\ \hline 30 \\ + 7 \\ \hline 37 \end{array} \qquad \begin{array}{r} 18 \\ + 25 \\ \hline 30 \\ + 43 \\ \hline 43 \end{array}$$

Dienes



$$38 - 12 = 26$$



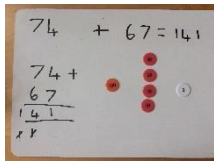
**Column Subtraction**

Model partitioning for expanded written method first.

$$\begin{array}{r} 38 \\ - 12 \\ \hline 26 \end{array}$$

## Key Stage 2 Addition and Subtraction Calculation Policy

Addition Year 3		Manipulatives	Subtraction Year 3		
Pictorial	Abstract		Pictorial	Abstract	
12 + 25 = 37		Counters Dienes Place Value Counters Place Value Cards 	38 - 12 = 26		
	<b>Column Addition</b> - Expand to include decimals  Model partitioning for expanded written method first.  $\begin{array}{r} 12 \\ + 25 \\ \hline 7 \\ \hline 30 \\ \hline 37 \end{array}$ $\begin{array}{r} 18 \\ + 25 \\ \hline 13 \\ \hline 30 \\ \hline 43 \end{array}$			<b>Column Subtraction</b> - Expand to include decimals  Model partitioning for expanded written method first.  $\begin{array}{r} 38 \\ - 12 \\ \hline 6 \\ \hline 20 \\ \hline 26 \end{array}$	
<b>Introduced by the end of Year 3</b>					
18 + 25 = 43	43 + 91 = 134	74 + 67 = 141	38 - 12 = 26	63 - 15 = 48	523 - 59 = 464
<b>Column Addition</b> - Use the language of carrying  $\begin{array}{r} 18 \\ + 25 \\ \hline 43 \end{array}$ $\begin{array}{r} 43 \\ + 91 \\ \hline 134 \end{array}$ $\begin{array}{r} 74 \\ + 67 \\ \hline 141 \end{array}$		Counters Dienes Place Value Counters Place Value Cards 	63 - 15 = 		<b>Column Subtraction</b> - Use the language of carrying  $\begin{array}{r} 38 \\ - 12 \\ \hline 26 \end{array}$ $\begin{array}{r} 63 \\ - 15 \\ \hline 48 \end{array}$ $\begin{array}{r} 523 \\ - 59 \\ \hline 464 \end{array}$
			63 - 15 = 		



Decimals:

$$\begin{array}{r} 3.5 \\ +2.4 \\ \hline 5.9 \end{array} \quad \begin{array}{r} 5.6 \\ +8.1 \\ \hline 13.7 \\ \phantom{0} \downarrow \end{array} \quad \begin{array}{r} 8.6 \\ +5.8 \\ \hline 13.4 \\ \phantom{0} \downarrow \phantom{0} \end{array}$$



Decimals:

$$\begin{array}{r} 6.7 \\ -2.4 \\ \hline 4.3 \end{array} \quad \begin{array}{r} \phantom{0}^3 4.15 \\ -\phantom{0}^3 2.8 \\ \hline \phantom{0}^3 1.7 \end{array} \quad \begin{array}{r} \phantom{0}^6 \phantom{0}^2 7.1310 \\ -\phantom{0}^6 \phantom{0}^2 4.73 \\ \hline \phantom{0}^6 \phantom{0}^2 2.57 \end{array}$$

**Column Subtraction-**  
(with multiple 0s)

$$\begin{array}{r} \phantom{0}^2 \phantom{0}^9 \phantom{0}^9 30010 \\ -\phantom{0}^2 \phantom{0}^9 \phantom{0}^9 697 \\ \hline \phantom{0}^2 \phantom{0}^9 \phantom{0}^9 2303 \end{array}$$

## Addition Year 4, 5, 6

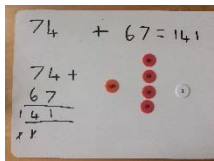
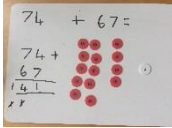
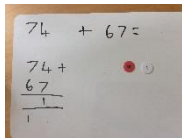
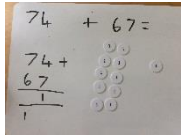
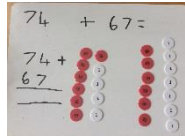
Pictorial

Abstract

$18 + 25 = 43$

$43 + 91 = 134$

$74 + 67 = 141$



### Column Addition -

Use the language of carrying

$$\begin{array}{r} 18 \\ + 25 \\ \hline 43 \\ \uparrow \end{array} \quad \begin{array}{r} 43 \\ + 91 \\ \hline 134 \\ \uparrow \end{array} \quad \begin{array}{r} 74 \\ + 67 \\ \hline 141 \\ \uparrow \uparrow \end{array}$$

Decimals:

$$\begin{array}{r} 3.5 \\ + 2.4 \\ \hline 5.9 \\ \hline \end{array} \quad \begin{array}{r} 5.6 \\ + 8.1 \\ \hline 13.7 \\ \uparrow \end{array} \quad \begin{array}{r} 8.6 \\ + 5. \\ \hline 13.4 \\ \uparrow \uparrow \end{array}$$

## Manipulatives

Counters

Dienes

Place Value Counters

Place Value Cards



## Subtraction Year 4, 5, 6

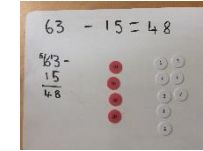
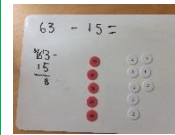
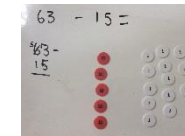
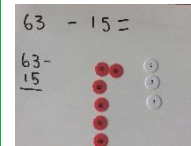
Pictorial

Abstract

$38 - 12 = 26$

$63 - 15 = 48$

$523 - 59 = 464$



### Column Subtraction-

Use the language of carrying

$$\begin{array}{r} 38 \\ - 12 \\ \hline 26 \end{array} \quad \begin{array}{r} 63 \\ - 15 \\ \hline 48 \end{array} \quad \begin{array}{r} 523 \\ - 59 \\ \hline 464 \end{array}$$






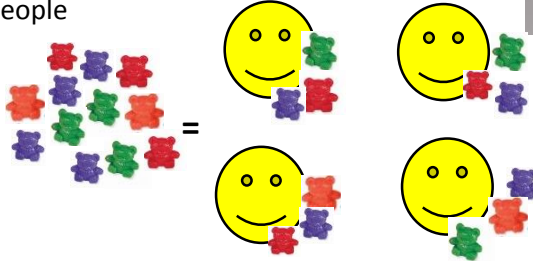
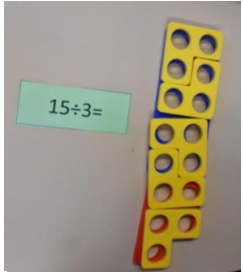
Decimals:

$$\begin{array}{r} 6.7 \\ - 2.4 \\ \hline 4.3 \end{array} \quad \begin{array}{r} 4.15 \\ - 2.8 \\ \hline 1.7 \end{array} \quad \begin{array}{r} 7.13 \\ - 4.73 \\ \hline 2.57 \end{array}$$

### Column Subtraction- (with multiple 0s)

$$\begin{array}{r} 300 \\ - 697 \\ \hline 2303 \end{array}$$

Key Stage 1 Multiplication and Division Calculation Policy

<p><b>Multiplication</b> <b>EYFS</b></p>	<p><b>Manipulatives</b></p>	<p><b>Division</b> <b>EYFS</b></p>
<p>Pictorial</p>		<p>Pictorial</p>
<p>Symbols/pictures/objects</p> <p>3 lots of 2 counters = <math>3 \times 2</math></p>  	<p>Counters Numicon Multi-link Compare bears Fingers Any objects</p>  	<p>Symbols/pictures/objects</p> <p>4 sticks shared between 2 children.</p>  <p>Sharing: share these bears between 4 people</p>  

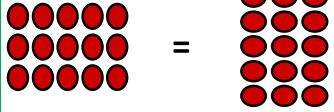
## Multiplication Year 1

Pictorial

Abstract

$5 \times 3 = 15$  or  $3 \times 5 = 15$  (commutative law\*)

Arrays:



$5 \times 3 = 3 \times 5$

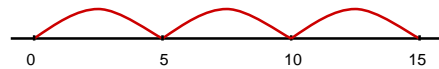
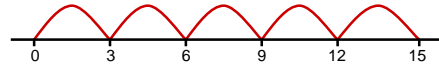
Numicon:



Dots/counters/cubes:



Repeated addition / number lines:



## Manipulatives

Counters

Number lines

Numicon

Multi-link

Compare bears

Fingers



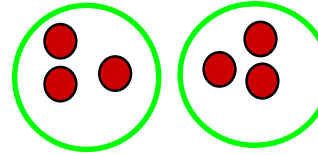
## Division Year 1

Pictorial

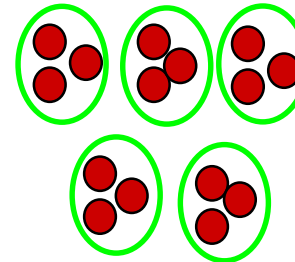
Abstract

$6 \div 3 = 2$        $15 \div 5 = 3$

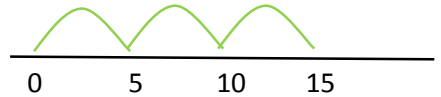
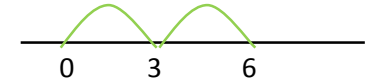
Grouping counters:


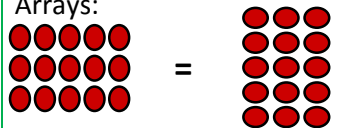
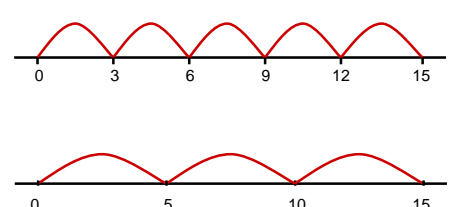
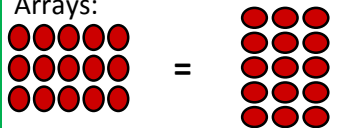
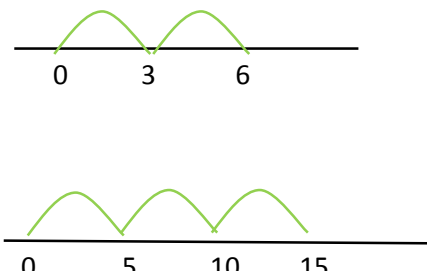






Sharing counters:



Repeated addition / number lines



Multiplication Year 2		Manipulatives	Division Year 2	
Pictorial	Abstract		Pictorial	Abstract
$5 \times 3 = 15$ or $3 \times 5 = 15$ (commutative law*)		Counters Number lines Numicon Multi-link Compare bears Fingers 	$6 \div 3 = 2$ $15 \div 5 = 3$	
Arrays:  $5 \times 3 = 3 \times 5$	Repeated addition / number lines: 		Arrays:  $5 \times 3 = 3 \times 5$	Repeated addition / number lines: 
Numicon:  Dots/counters/cubes: 		Numicon:  Dots/counters/cubes: 		

- Commutative Law: where the numbers can be in any order and still produce the same answer

e.g.  $6 \times 5 = 30$        $5 \times 6 = 30$

$4 + 9 = 13$        $9 + 4 = 13$



Key Stage 2 Multiplication and Division Calculation Policy

Multiplication Year 3		Manipulatives	Division Year 3																																
Pictorial	Abstract		Pictorial	Abstract																															
$43 \times 6 = 258$		<p>Counters Dienes Place Value Counters Place Value Cards</p>	$36 \div 3 = 12$																																
<p><b>Short Multiplication</b> – ensure pupils can partition into tens and ones before introducing grid Expand to include decimals (times tables are crucial for this method)</p> <p>Grid:</p> <table border="1" style="margin-left: 40px;"> <tr><td>x</td><td>6</td></tr> <tr><td>40</td><td>240</td></tr> <tr><td>3</td><td>18</td></tr> <tr><td></td><td>258</td></tr> </table>			x	6	40	240	3	18		258	<p><b>Long method</b> – chunking then move to compact Expand to include decimals Expanded (times tables are crucial for this method)</p> <div style="text-align: right; margin-right: 50px;"> <table style="border-collapse: collapse;"> <tr><td></td><td>1</td><td>2</td></tr> <tr><td>3</td><td>3</td><td>6</td></tr> <tr><td></td><td>3</td><td>0</td></tr> <tr><td colspan="3"><hr/></td></tr> <tr><td></td><td>6</td><td></td></tr> <tr><td></td><td>6</td><td></td></tr> <tr><td colspan="3"><hr/></td></tr> <tr><td></td><td>0</td><td></td></tr> </table> </div>			1	2	3	3	6		3	0	<hr/>				6			6		<hr/>				0
x	6																																		
40	240																																		
3	18																																		
	258																																		
	1	2																																	
3	3	6																																	
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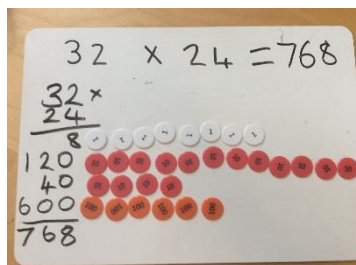
By the end of Year 3 introduce expanded multiplication in Year 4 section

## Multiplication Year 4

Pictorial

Abstract

$$32 \times 24 = 768$$



### Long Multiplication

Expand to include decimals  
(times tables are crucial for this method)

Expanded:

$$\begin{array}{r} 32 \\ 24 \times \\ \hline 8 \\ 120 \\ 40 \\ 600 \\ \hline 768 \end{array}$$

Progressing onto compact:

$$\begin{array}{r} 32 \\ 24 \times \\ \hline 128 \\ 640 \\ \hline 768 \end{array}$$

*Order of calculation*

*u x u (4x2)*

*u x t (4x3)*

*t x u (2x2)*

*t x t (2x3)*

## Manipulatives

Counters

Dienes

Place Value Counters

Place Value Cards



## Division Year 4

Pictorial

Abstract

$$570 \div 5 = 114$$


**Short Method** (for number divide by a 1 digit number)

Expand to include decimals

Use the language of exchanging

(times tables are crucial for this method)

$$\begin{array}{r} 114 \\ 5 \overline{) 570} \end{array}$$

<b>Multiplication</b> <b>Year 5 and 6</b>	<b>Manipulatives</b>	<b>Division</b> <b>Year 5 and 6</b>
Abstract		Abstract
$32 \times 24 = 768$	Counters Dienes Place Value Counters Place Value Cards	$570 \div 5 = 114$
<p><b>Long Multiplication</b>            Expand to include decimals            (times tables are crucial for this method)</p> $  \begin{array}{r}  32 \\  24 \times \\  \hline  128 \\  640 \\  \hline  768  \end{array}  $ <p>Order of calculation  <math>u \times u</math> (4x2)  <math>u \times t</math> (4x3)  <math>t \times u</math> (2x2)  <math>t \times t</math> (2x3)</p>		<p><b>Short Method</b> (for number divide by a 1 digit number)            Expand to include decimals            Use the language of exchanging            (times tables are crucial for this method)</p> $  \begin{array}{r}  114 \\  5 \overline{) 570}  \end{array}  $
$9.3 \times 54 = 483.6$ (decimals)		$684 \div 19 = 36$
$  \begin{array}{r}  9.3 \\  \times 54 \\  \hline  372 \\  4650 \\  \hline  502.2  \end{array}  $ <ol style="list-style-type: none"> <li>Line up the two numbers forgetting about the PV columns</li> <li>Pretend the decimal point(s) aren't there and treat them as whole numbers.</li> <li>Work out exactly the same way as if they were whole numbers.</li> <li>Vertically add the numbers generated.</li> <li>Count how many numbers are to the right of the decimal in the original multiplication (the 3 therefore 1 number).</li> <li>Then put a decimal place back into your answer, depending on how many you counted in step 5 (in the instance it's 1). Counting from the right.</li> </ol>		<p><b>Long method</b> (for number divide by a 2 digit number)            Expand to include decimals            Expanded            (times tables are crucial for this method)</p> $  \begin{array}{r}  36 \\  19 \overline{) 684} \\  \underline{190} \quad (10 \times 19) \\  494 \\  \underline{380} \quad (20 \times 19) \\  114 \\  \underline{95} \quad (5 \times 19) \\  19 \\  \underline{19} \quad (1 \times 19) \\  00  \end{array}  $

For videos to help with manipulatives and method go to:

<https://www.youtube.com/user/NCETM>